

MECA-H-406 Composite structures - Exercises 2

1. Consider a unidirectional composite (circular fibers) with $E_f=70\text{GPa}$, $E_m=3.5\text{GPa}$ and $V_f=70\%$.

- (a) A transversal stress of 90MPa induces a longitudinal deformation $\epsilon_L=-2.1\text{e-}4$. Compute the major Poisson's ratio, ν_{LT} .
- (b) Compute σ'_{LU} assuming that the tensile and compressive Young's moduli are assumed identical and that $\sigma_{mu}=48\text{MPa}$.

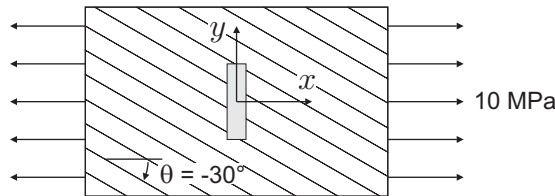
2. In order to reduce the mass of a simply-supported aluminium beam of length L , we consider changing its material for a unidirectional composite ply. This beam is subjected to a temperature gradient Δt between its top and bottom faces.

- (a) Show that such a temperature gradient is equivalent to a pair of moments given by $M = EI\alpha\Delta t/h$ applied to its ends, where E is the Young's modulus, α is the coefficient of thermal expansion, I is the bending inertia and h is the thickness. We suppose that the beam obeys Euler-Bernoulli hypotheses and we neglect the Poisson's effects.
- (b) Using the numerical values below, compute the maximum deflection of the beam.
 $\Delta t=110\text{K}$, $L=3.5\text{m}$, $h=0.1\text{m}$, $b=0.1\text{m}$.

aluminium	$\alpha = 44.10^{-6} \text{ 1/K}$	$E=71\text{GPa}$
Kevlar - epoxy	$\alpha_L = -8.10^{-6} \text{ 1/K}$	$E_L=86\text{GPa}$
graphite - epoxy	$\alpha_L = 4.10^{-6} \text{ 1/K}$	$E_L=201\text{GPa}$

3. What is the strain (ϵ_y) measured by the gauge glued on the ply below ?

$E_L=100 \text{ GPa}$, $E_T=10 \text{ GPa}$, $\nu_{LT}=0.3$, $G_{LT}=6 \text{ GPa}$.



4. Consider a unidirectional composite ply with $h=0.25\text{mm}$, $E_L=120 \text{ GPa}$, $E_T=8.5 \text{ GPa}$, $\nu_{LT}=0.29$, $G_{LT}=3 \text{ GPa}$.

Plot the evolution of the components of the stiffness matrix $[\bar{Q}]$ as a function of the orientation of the fibers, θ . Comment.

